# Comparison of the Astrometric Measurements of SHJ355 and STF3022 Obtained with Different Techniques and Software 

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#### Abstract

Astrometric measurements of Sh355 and STF3022 are reported along with standard deviations. Evaluation on the alignment of the images with IRIS 5.59 (by Christian Buil) and comparison between the average data obtained and the data obtained from the image are also discussed. Comparison of results obtained through the use of IRIS 5.59 and REDUC 3.88 (by Florent Losse) is presented.


## Description of the Stellar Systems Studied and Methods

Sh355 (WDS 23300+5833 SHJ355: J2000 RA 23 h 30 m 01.92 s ; DEC $58^{\circ} 32^{\prime} 56.1^{\prime \prime}$ ) is a nice multiple system in Cassiopeia, whose main component has a blue tint (B3IV). The system has 8 components, where pairs $A B$ and $C D$ are difficult and very unbalanced. Therefore, in this study, we analyzed the system for only the six visual components. F and G, again form a double star (HJ 1887) while component I, belongs to a system attributed to Burnham in 1906 (BU 1149).

In the same field of the CCD another system is visible: STF3022 (WDS 23309+5825STF3022: J2000 AR 23 h 30 m 52.02 s ; DEC $58^{\circ} 24^{\prime} 56.5^{\prime \prime}$ ). This is actually a triple star.

The telescope used was a Newtonian SkyWatcher 200/1000 on a EQ6 SkyScan German equatorial mount. Attached to the telescope was a MAGZERO MZ-5m CCD camera and MPCC Baader Planetarium coma corrector .

In Figure 1, you can see the CCD field with the systems SHJ355 and STF3022.

## Image Capture and Data Analysis

Two software packages, IRIS 5.59 and REDUC 3.88, were used to analyze the images to determine the precision and accuracy of both.

IRIS 5.59 (by Christian Buil), will perform an astrometric reduction of a CCD field (using GSCACT as a reference) and the software implements a useful function to correct optic distortions.

The positions of the stars in the GSC-ACT catalog, have a stated accuracy of $0.2^{\prime \prime}$ and therefore the goal is to stay in this range.

We did an astrometric measurement of 9 stars on 10 images, plus other 9 measurements on the mean image for a total of 99 measurements of coordinates. Table 1 shows the mean of the 10 astrometric measurements. Table 2 shows the measurements taken from the mean image.

As can be seen in Figure 2 and from a comparison with Table 1 and Table 2, the mean measurements have minimal differences, compared with direct measurements on the mean image.

We have, therefore, an error less than one tenth

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Table 1: Mean of 10 Astrometric Measurements Using IRIS 5.59

| ID | RA | Dec |
| :---: | :---: | :---: |
| Sh355 Ab | 23h 30m 02.073s | +58 ${ }^{\circ} 32$ '56.67" |
| Sh355 Cd | 23h 29m 52.354s | +58 ${ }^{\circ} 32^{\prime} 54.72^{\prime \prime}$ |
| Sh355 E | 23h 30m 06.601s | +58 32 '38.37" |
| Sh355 F | 23h 29m 58.849s | +58 ${ }^{\circ} 33^{\prime} 58.84{ }^{\prime \prime}$ |
| Sh355 G | 23h 30m 00.167s | +58 ${ }^{\circ} 34^{\prime} 01.92^{\prime \prime}$ |
| Sh355 I | 23h 29m 48.461s | +58 ${ }^{\circ} 29^{\prime} 31.27^{\prime \prime}$ |
| STF3022 A | 23h 30m 52.134s | +58 ${ }^{\circ} 24^{\prime} 57.01^{\prime \prime}$ |
| STF3022 B | 23h 30m 50.243s | +58 ${ }^{\circ} 24^{\prime} 42.96{ }^{\prime \prime}$ |
| STF3022 C | 23h 30m 49.371s | +58 ${ }^{\circ} 23^{\prime} 01.41^{\prime \prime}$ |

Table 2: Measurements on the mean image of the 10 images using IRIS 5.59

| ID | RA | Dec |
| :---: | :---: | :---: |
| Sh355 Ab | 23h 30m 02.073s | +58 ${ }^{\circ} 32^{\prime} 56.64{ }^{\prime \prime}$ |
| Sh355 Cd | 23h 29m 52.359s | +58 ${ }^{\circ} 32^{\prime} 54.75^{\prime \prime}$ |
| Sh355 E | 23h 30m 06.598s | +58 ${ }^{\circ} 32^{\prime} 38.33^{\prime \prime}$ |
| Sh355 F | 23h 29m 58.854s | +58 ${ }^{\circ} 33^{\prime} 58.84^{\prime \prime}$ |
| Sh355 G | 23h 30m 00.169s | +58³ $34^{\prime} 01.86{ }^{\prime \prime}$ |
| Sh355 I | 23h 29m 48.478s | +58 ${ }^{\circ} 29^{\prime} 31.29^{\prime \prime}$ |
| STF3022 A | 23h 30m 52.136s | +58 ${ }^{\circ} 24^{\prime} 56.99^{\prime \prime}$ |
| STF3022 B | 23h 30m 50.245s | +58 ${ }^{\circ} 24^{\prime} 42.94^{\prime \prime}$ |
| STF3022 C | 23h 30m 49.376s | +58 ${ }^{\circ} 23^{\prime} 01.35^{\prime \prime}$ |

WDS $23300+5833$ SHJ355
J2000: AR $23 \mathrm{~h} 30 \mathrm{m01.92s}$; DEC 58³2'56.1"


Figure 1: CCD field with the systems SHJ355 (upper right) and STF3022.


Figure 2: Difference Between the Data of Tables 1 and 2.

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Table 3: Summary data on meaon of 10 measurements with the separation in arc seconds and the relative standard deviations.

| Rho | SH355 CD | SH355 E | SH355 F | SH355 G | SH355 I |
| :---: | :---: | :---: | :---: | :---: | :---: |
| SH355 AB | 76.088 | 39.881 | 67.091 | 66.937 | 231.422 |
| SH355 CD |  | 112.698 | 81.815 | 90.847 | 205.720 |
| SH355 E |  |  | 100.764 | 97.544 | 234.943 |
| SH355 F |  |  |  | 10.761 | 279.659 |
| SH355 G |  |  |  |  | 285.754 |
| Rho | STF3022 B | STF3022 C |  |  |  |
| STF3022 A | 20.449 | 117.622 |  |  |  |
| STF3022 B |  | 101.781 |  |  |  |
|  |  |  |  |  |  |
| Std. Dev. Rho | SH355 CD | SH355 E | SH355 F | SH355 G | SH355 I |
| SH355 AB | 0.077 | 0.079 | 0.060 | 0.062 | 0.097 |
| SH355 CD |  | 0.082 | 0.089 | 0.080 | 0.091 |
| SH355 E |  |  | 0.047 | 0.041 | 0.070 |
| SH355 F |  |  |  | 0.034 | 0.045 |
| SH355 G |  |  |  |  | 0.060 |
| Std. Dev. Rho | STF3022 B | STF3022 C |  |  |  |
| STF3022 A | 0.041 | 0.056 |  |  |  |
| STF3022 B |  | 0.068 |  |  |  |

Table 4: Summary data of the mean of 10 measurements of the postion angle and the relative standard deviations.

of an arc-second.
Table 3 shows the summary data of the mean of 10 measurements with the separation in arc-seconds and the relative standard deviations. In Table 4 is the summary data of the mean of 10 measurements of the position angle and the relative standard deviations. Analyzing the data, we found that the standard deviations of Theta, are more or less inversely proportional to Rho.

With IRIS, calibration and image orientation are obtained with trigonometry of two distant points of the mean image. The calibration data obtained are Sampling $\Sigma=1.072572$ a.s. / pixel and Orientation $\Delta=0.211^{\circ}$

With REDUC, instead, to make measurements you need to calibrate the image on a pair of stars with known measures to find the orientation and sampling.
Tables 5 and 6 show the data obtained with IRIS 5.59 and with REDUC 3.88.

In Figures 3 and 4, one can evaluate the performance of the two software packages. Figure 3 shows the values of position angle: theta values obtained with IRIS are shown in blue and theta values obtained with REDUC are shown in red.

Similarly, Figure 4 shows the values of separation in arc-seconds; yellow points are from IRIS and green points from REDUC.
From these two graphs, we note that the position angle values are similar. This is not the case for separation where the error increases with the absolute value of the measurement and the relative error, $\Delta$ Rho / Rho, is around $1 \%$ for all data.

## Comparison with the Official Data of Different Catalogs

The data obtained with IRIS and REDUC were compared with the most important catalogs. Table 7 shows the data from the Washington Double Star Catalog, UCAC3 (The third US Naval Observatory CCD Astrograph Catalog, 2009), and PPMXL (Catalog of Positions and Proper Motions on the ICRS, 2010).

Analyzing the data in Table 8, we can see that IRIS has a maximum relative error,

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Table 5: Data Obtained with IRIS 5.59

| NAME | RA+DEC | MAGS | PA | ST. DEV. <br> PA | SEP. | ST. DEV. <br> SEP. | DATE | N |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| NOTES |  |  |  |  |  |  |  |  |
| SHJ 355AbCd | $23300+5833$ | $4.87-7.23$ | 268.53 | 0.04 | 76.088 | 0.077 | 2010.772 | 1 |
| SHJ 355AbE | $23300+5833$ | $4.87-11.28$ | 117.31 | 0.12 | 39.881 | 0.079 | 2010.772 | 1 |
| SHJ 355AbF | $23300+5833$ | $4.87-10.59$ | 337.91 | 0.07 | 67.091 | 0.060 | 2010.772 | 1 |
| SHJ 355AbG | $23300+5833$ | $4.87-11.11$ | 347.12 | 0.09 | 66.937 | 0.062 | 2010.772 | 1 |
| SHJ 355AbI | $23300+5833$ | $4.87-9.87$ | 207.41 | 0.02 | 231.422 | 0.097 | 2010.772 | 1 |
| SHJ 355FG | $23300+5834$ | $10.59-11.11$ | 73.33 | 0.24 | 10.761 | 0.034 | 2010.772 | 1 |
| STF3022AB | $23309+5825$ | $8.34-9.94$ | 226.6 | 0.09 | 20.449 | 0.041 | 2010.772 | 1 |
| STF3022AC | $23309+5825$ | $8.34-9.5$ | 190.64 | 0.06 | 117.62 | 0.056 | 2010.772 | 1 |

Table 6: Data obtained with REDUC 3.88.

| NAME | RA+DEC | MAGS | PA | DEV.ST. <br> A | SEP. | DEV.ST. <br> SEP. | DATE | N |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| NOTES |  |  |  |  |  |  |  |  |
| SHJ 355AbCd | $23300+5833$ | $4.87-7.23$ | 268.42 | 0.04 | 76.768 | 0.070 | 2010.772 | 1 |
| SHJ 355AbE | $23300+5833$ | $4.87-11.28$ | 117.15 | 0.26 | 40.308 | 0.158 | 2010.772 | 1 |
| SHJ 355AbF | $23300+5833$ | $4.87-10.59$ | 337.88 | 0.10 | 67.781 | 0.170 | 2010.772 | 1 |
| SHJ 355AbG | $23300+5833$ | $4.87-11.11$ | 347.08 | 0.06 | 67.666 | 0.082 | 2010.772 | 1 |
| SHJ 355AbI | $23300+5833$ | $4.87-9.87$ | 207.31 | 0.03 | 233.606 | 0.122 | 2010.772 | 1 |
| SHJ 355FG | $23300+5834$ | $10.59-11.11$ | 73.09 | 0.64 | 10.862 | 0.143 | 2010.772 | 1 |
| STF3022AB | $23309+5825$ | $8.34-9.94$ | 226.32 | 0.20 | 20.707 | 0.041 | 2010.772 | 1 |
| STF3022AC | $23309+5825$ | $8.34-9.5$ | 190.64 | 0.06 | 118.898 | 0.055 | 2010.772 | 1 |

Table 7: Data obtained with IRIS and REDUC compared with the most important catalogs.

|  | SHJ355 AC |  | SHJ 355 AE |  | SHJ355 FG |  | STF3022 AB |  | STF3022 AC |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | rho | theta | rho | theta | rho | theta | rho | theta | rho | theta |
| WDS | 75.860 | 268.5 | 40.480 | 116.8 | 10.790 | 72.9 | 20.330 | 226.1 | 117.630 | 190.4 |
| UCAC3 (2009) | 75.615 | 268.76 | 40.582 | 116.6 | 10.718 | 73.24 | 20.410 | 226.26 | 117.705 | 190.48 |
| PPMXL (2010) | 75.655 | 268.74 | 40.580 | 116.7 | 10.787 | 72.91 | 20.451 | 226.33 | 117.807 | 190.49 |
| mean IRIS | 76.088 | 268.53 | 39.881 | 117.31 | 10.761 | 73.33 | 20.449 | 226.6 | 117.620 | 190.64 |
| mean REDUC | 76.768 | 268.42 | 40.308 | 117.15 | 10.862 | 73.09 | 20.707 | 226.32 | 118.898 | 190.64 |

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Figure 3: Comparison of the values of theta between IRIS and Reduc.


Figure 4: Comparison of the values of rho between IRIS and Reduc.

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Table 8: margin of error expressed as \% error.

|  | SHJ355 AC |  | SHJ 355 AE |  | SHJ355 FG |  | STF3022 AB |  | STF3022 AC |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | rho | theta | rho | theta | rho | theta | rho | theta | rho | theta |  |  |
| Mean of UCAC3 \& PPMXL data | 75.635 | 268.750 | 40.581 | 116.650 | 10.753 | 73.075 | 20.431 | 226.295 | 117.756 | 190.485 |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | e\% | e\% | e\% | e\% | e\% | e\% | e\% | e\% | e\% | e\% | mean e\% | $\begin{array}{\|c} \hline \text { St. dev. } \\ \text { e\% } \end{array}$ |
| WDS | 0.30 | 0.09 | 0.25 | 0.13 | 0.35 | 0.24 | 0.49 | 0.09 | 0.11 | 0.04 | 0.21 | 0.14 |
| Mean IRIS | 0.60 | 0.08 | 1.76 | 0.56 | 0.08 | 0.35 | 0.09 | 0.13 | 0.12 | 0.08 | 0.38 | 0.52 |
| Mean REDUC | 1.48 | 0.12 | 0.68 | 0.43 | 1.01 | 0.02 | 1.34 | 0.01 | 0.96 | 0.08 | 0.61 | 0.56 |

(Continued from page 146)
while REDUC has the highest average error rate.
In both cases the data are certainly consistent with the Washington Double Star Catalog.

## Conclusions

The two different methods software packages yielded values of Theta and Rho that were very similar. The separation (Rho) values had a relative error of $1 \%$, while the position angle (Theta) values had a relative error around $0.2^{\circ}$.

IRIS and standard astrometric method should be more accurate when the double star is quite large, and a non-linear approximation of the entire star field is needed. For example, a coma corrector can cause distortion of the field, which IRIS can correct, as opposed to REDUC.

REDUC, for its simplicity, seems more appropriate for all other cases, when the component stars are close or very close. In these cases IRIS has some difficulty in managing the centroid and the error can be higher. REDUC should be a good choice when using
small CCD too, when the field distortion can be ignored.

The performance of IRIS can be best with most recent star catalogs (UCAC3 or PPMXL).

## References

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